



The Golden Age of Statistical Maps & Diagrams

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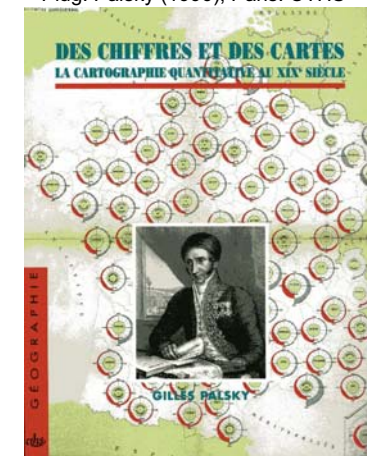
Chicago Maps Society, Dec. 12, 2007

Slides: www.math.yorku.ca/SCS/Papers/maps/

Acknowledgements: Thanks!

- Bob Karrow, Jim Akerman: *Maps* book
- Co-author: Gilles Palsky, Univ. Paris 1.
- Arthur H. Robinson: mentor-by-email
- *Chevaliers des Album de Statistique Graphique*:
 - Antoine de Falguerolles, Ian Spence, Howard Wainer, Ruddy Osterman, Tom Koch, Stephen Stigler, ...

Plug: Palsky (1996), Paris: CTHS



2

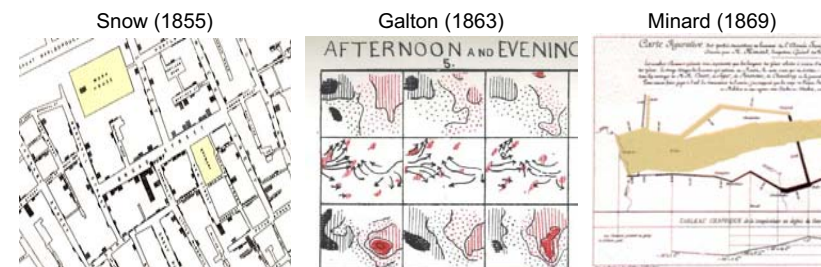
Outline

- Introduction
 - Data visualization: thematic maps & diagrams
 - Context: Milestones Project
 - What is an Age? Why is it Golden?
- Preludes to the Golden Age
 - Statistics: Numbers of the state
 - Statistical theory, technology
 - Inventions in statistical graphics & cartography
- Exemplars of the Golden Age
 - Graphic vision of Charles Joseph Minard
 - Francis Galton's graphic discoveries
 - Statistical atlases

3

Data visualization: thematic maps & diagrams

- Different 'visual language', but common goals:
 - **Exploration**: show trends, reveal patterns in quantitative or qualitative info
 - **Analysis**: aid in synthesizing, generalizing or testing patterns
 - **Presentation**: stimulate thought, convey conclusions, argue a point

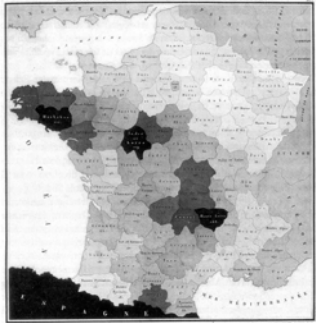


4

Data visualization: Diffusion of ideas

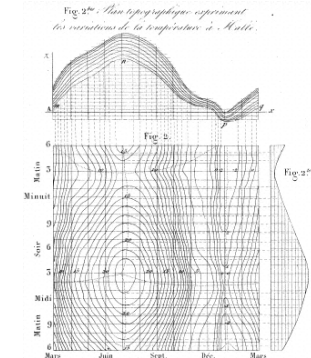
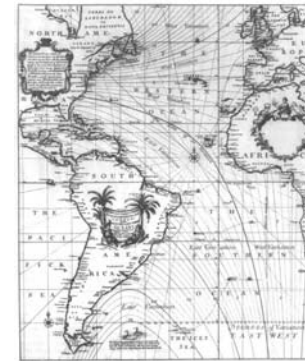
- Men who developed thematic maps often not cartographers

Dupin (1826): literacy in France Galton (1881): travel time from London



Data visualization: Diffusion of ideas

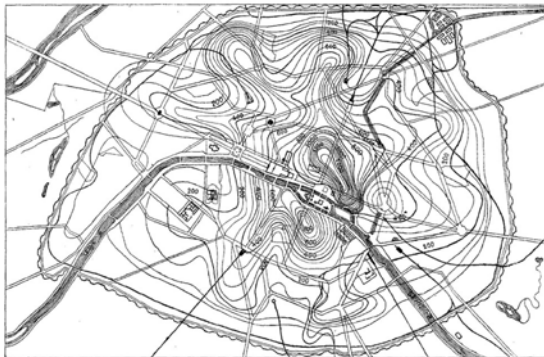
- Men who developed data graphics often borrowed from cartography
 - Halley (1701): contour map -> Lalanne (1843): contour diagrams of soil temp



6

Data visualization: Diffusion of ideas

- ... and vice-versa
 - Lalanne → L.L. Vauthier (1874) contour map of population density of Paris



7

Data visualization: Diffusion of ideas

- Graphical inventions often applied to maps
 - Playfair (1805): pie chart -> Minard (1858): pie map

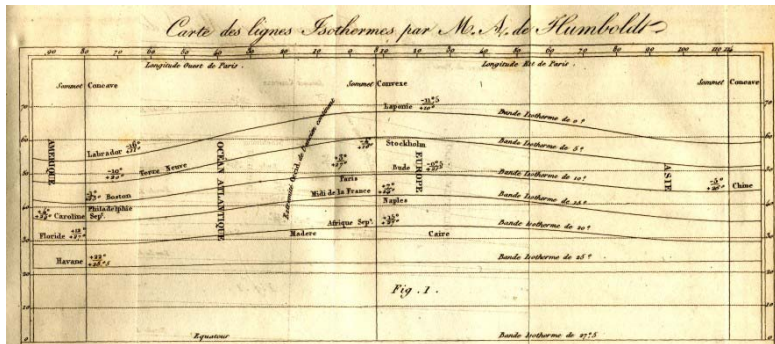


8

Data visualization: Diffusion of ideas

- In map-based graphics, the map was often secondary: background, or deformed to fit the data

A. von Humboldt (1817): Lines of isotherms

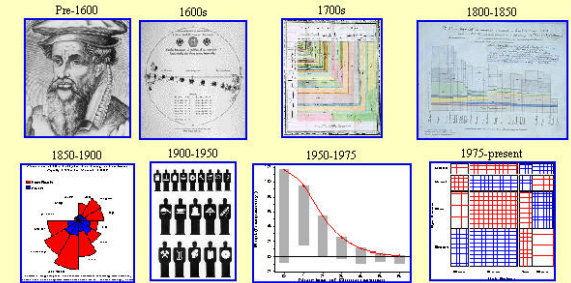


9

Context: Milestones Project

www.math.yorku.ca/SCS/Gallery/milestone

Milestones in the History of Thematic Cartography, Statistical Graphics, and Data Visualization



An illustrated chronology of innovations by Michael Friendly and Daniel J. Denis

Up: Gallery Introduction Related References Term Index Category XRef Search

Pre-1600 1600s 1700s 1800+ 1850+ 1900+ 1950+ 1975+

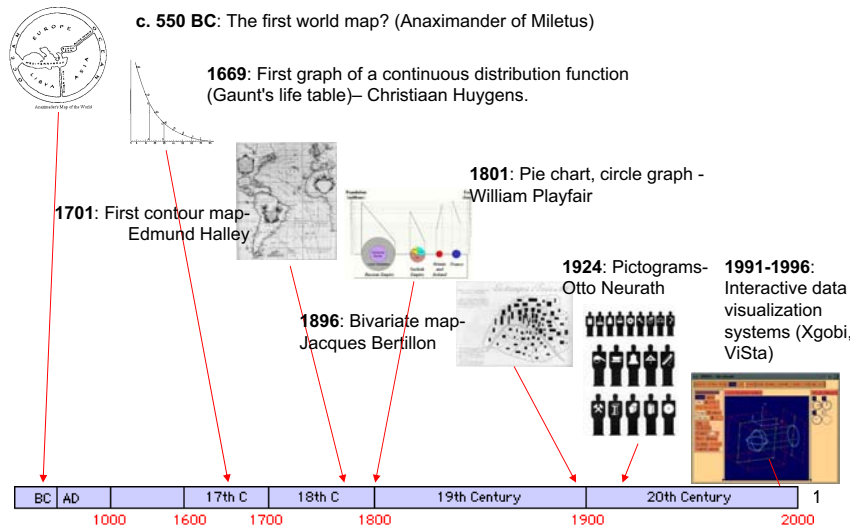
Project goals:

- Comprehensive catalog of developments in history of data visualization
- Tool to study themes, antecedents, influences, patterns, trends, etc.

10

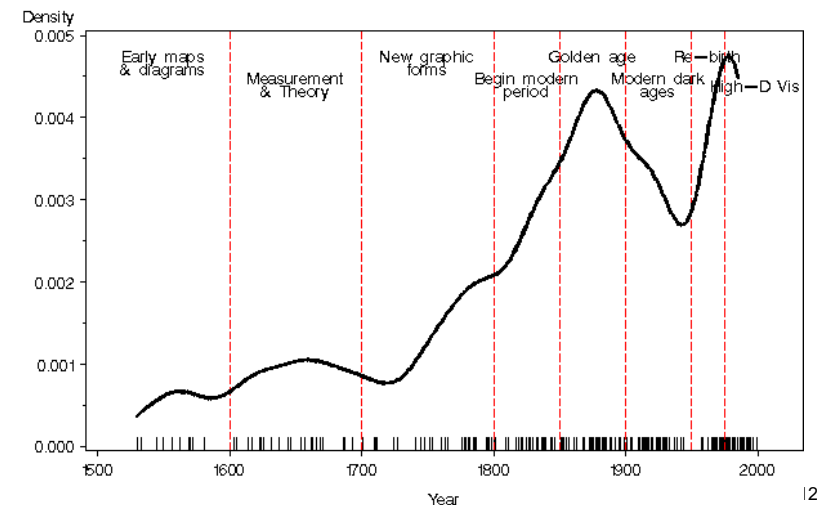
Milestones: Content Overview

Every picture has a story – Rod Stewart



Milestones as a graph

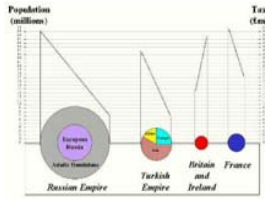
Milestones: Time course of developments



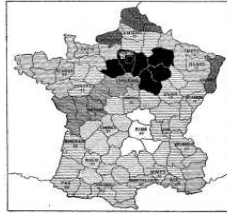
12

1800-1849: Beginning of modern data graphics

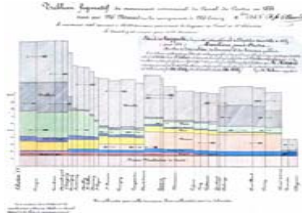
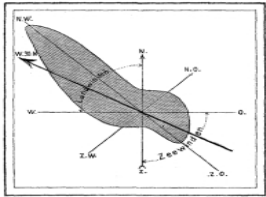
1801: Pie chart, circle graph invented- William Playfair



1819: First modern statistical map (illiteracy in France)- Charles Dupin



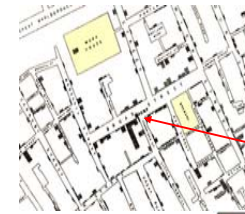
1843: Wind-rose (polar coordinates)- L. Lalanne



1844: variable-width, divided bars, area ~ cost of transport- C. J. Minard



1850-1900: Golden Age



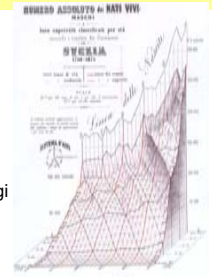
1855: Dot map of disease data (cholera)- John Snow

Broad St. pump

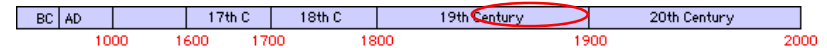
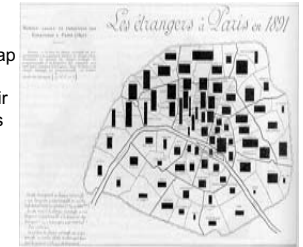
1884: Recursive multi-mosaic on a map- Emile Cheysson



1879: Stereogram (3D population pyramid)- Luigi Perozzo



1896: Area rectangles on a map to display two variables and their product- Jacques Bertillon



What makes an "Age"? Why is it "Golden"?

- Age:
 - Qualitatively distinct from before & after
- Golden age:
 - Recognizable period in a field where great tasks were accomplished
 - Years following some innovations
 - Artists apply skills to new areas
 - New ideas expressed, art forms flourish
 - Often ends with some turning point event(s)

Some Golden Ages

- Athens (Pericles): 448 BC—404 BC
- Islam: 622—1258 (sack of Baghdad)
- England: Elizabeth I
- Piracy: 1690--1730
- Radio: 1920—1940
- Animation: 1928 (sound) – 1960s (TV)
- Senior citizens: 60+



Pietro Da Cortona, *The Golden Age* (Fresco)¹⁶
Sala della Stufa, Palazzo Pitti, Florence)

Preludes to the Golden Age

- Data: collection & dissemination
- Statistical theory: combining & summarizing quantitative information
- Technology: printing & reproduction of maps & diagrams
- Visual language: new graphic forms for maps and diagrams
- → a perfect storm for data graphics

17

Preludes: data

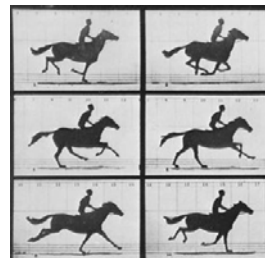
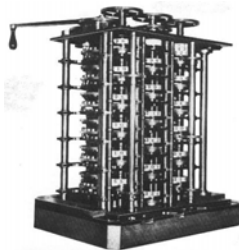
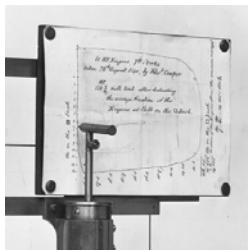
"Data! Data! I can't make bricks without clay." – Sherlock Holmes, Copper Beeches

- Population: ~ 1660--
 - Bills of mortality: Graunt (1662)
 - Political arithmetic: Petty (1665)
 - Demography: Süssmilch (1741)
- Economic data: ~ 1770--
 - Revenue, expenditures, taxes
 - Imports, exports
 - Transport
- Social data: ~ 1820--
 - Literacy, education
 - Crime, suicides, illegitimate births, prostitution
 - Poverty, debtors, disease
- → An avalanche of data, waiting to be visualized!

18

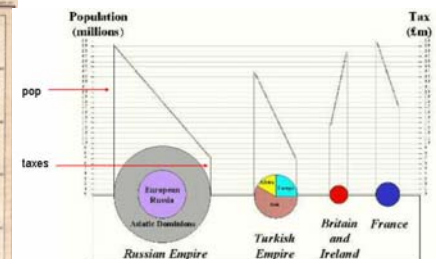
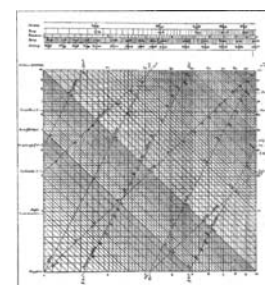
Preludes: technology

- Copperplate → Lithography (1800+) → color printing (1850+)
- Automatic recording: James Watt (1822)
- Calculation: Babbage (1822/33)
- Photography: Niépce (1827), Deguerre (1839), trichromatic process (1861)
- Motion: Muybridge (1872), Marey (1882)



Preludes: visual language

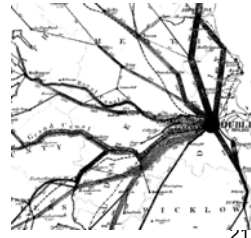
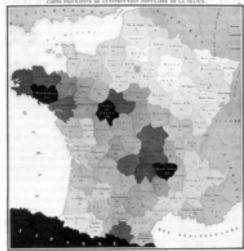
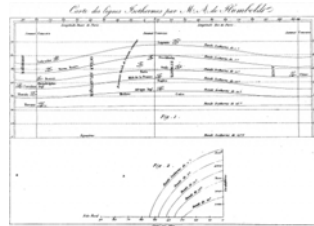
- Graphs & diagrams
 - Line, bar, pie charts– Playfair (1786, 1801)
 - Scatterplot– Herschel (1832)
 - Polar plots– Guerry (1829), Nightingale (1857)
 - Nomograms & graphical calculation– Lalanne (1846)



Preludes: visual language

• Maps

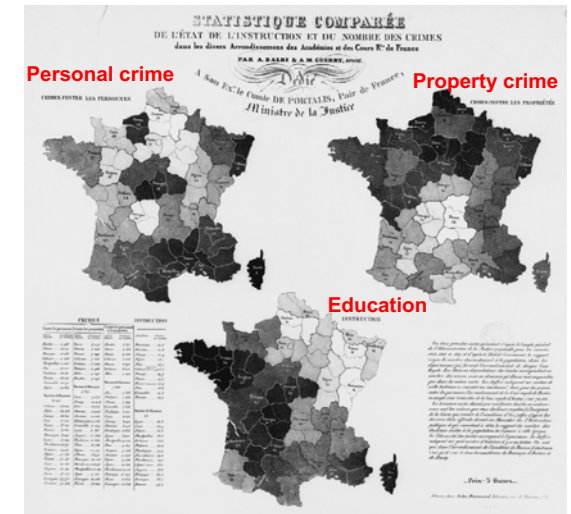
- Isopleth– Humboldt (1817)
- Choropleth– Dupin (1826)
- Dot– Frère de Montizon (1830)
- Flow– Harness (1837)



- Comparative & analytic maps (Balbi & Guerry, 1829)

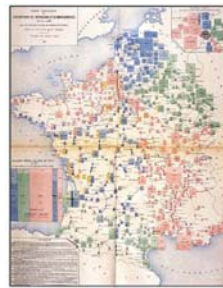
First comparative maps of social data (crime, education)

- personal crime inversely related to property crime!
- neither directly related to education!
- Education: *France obscure* vs. *France éclairée*

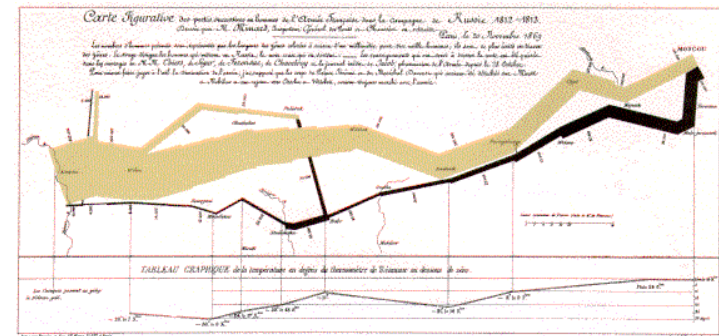


Exemplars of the Golden Age

- The graphic vision of C. J. Minard
- Galton's graphic discoveries
- State statistical albums



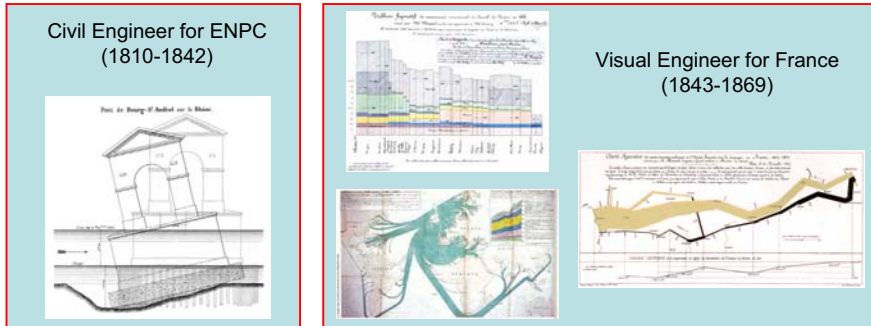
The graphic vision of C. J. Minard



- Marey (1878): “defies the pen of the historian in its brutal eloquence”
- Tufte (1983): “the best statistical graphic ever produced”

Why Minard?

- Study breadth and depth of his work
 - How related to work in his time?
 - How related to modern statistical graphics?
 - How related to his personal history?

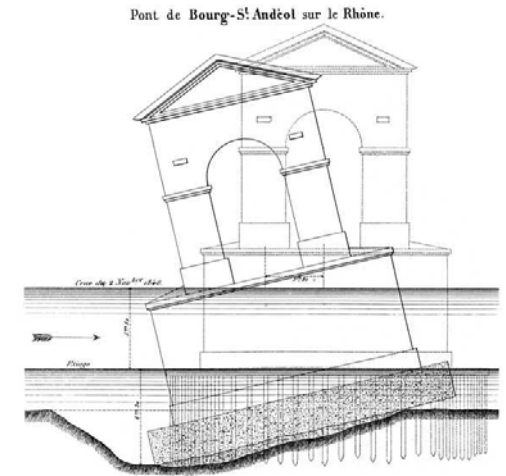


25

Visual thinking, visual explanation

1840: Why did the bridge at Bourg-St. Andéol collapse?

Minard's report consisted essentially of this self-explaining diagram.



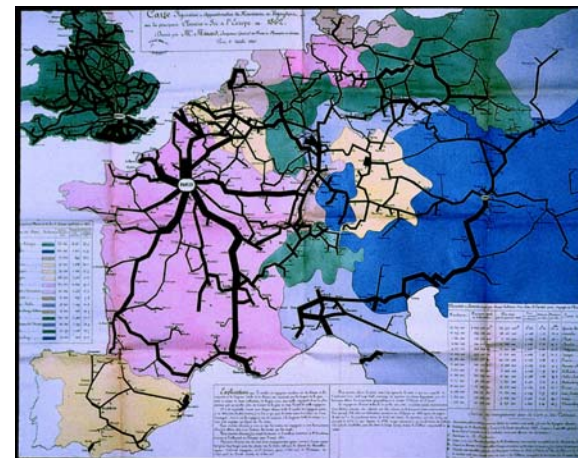
Visual tools for state planning

- 1830—1860: emergence of modern French state, dawn of globalization
- Trade, commerce, transportation:
 - Where to build railroads, canals?
 - Visualizing changes over time, differences over space
 - → Flow maps and other graphical innovations

27

Flow maps as visual tools

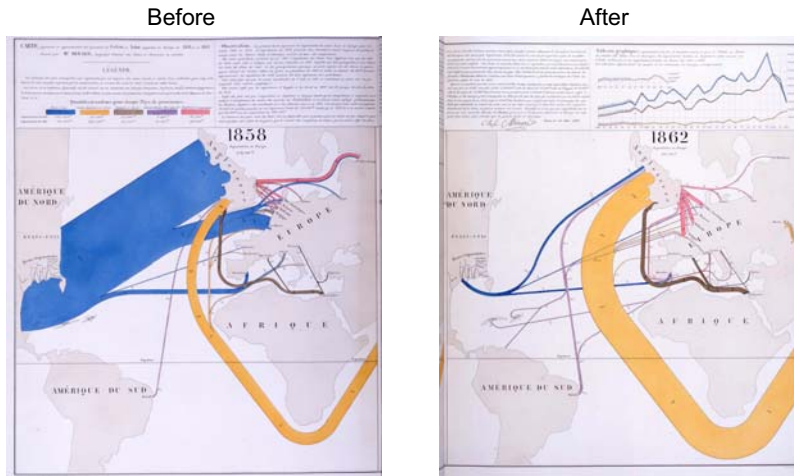
Transport of passengers on the principal railroads in Europe in 1862



Carte figurative: give precedence to the data over the map

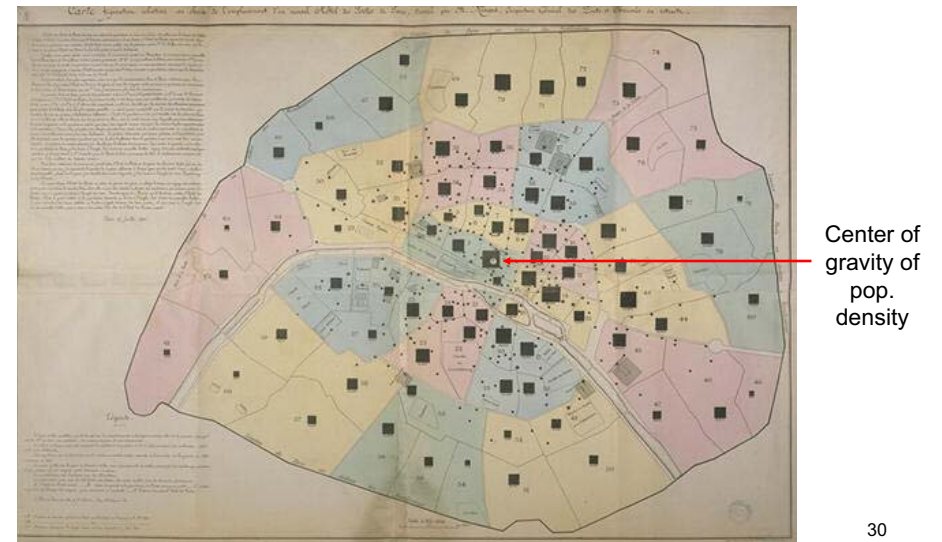
28

Effect of US civil war on cotton trade



29

Where to build a new post office?(1867)

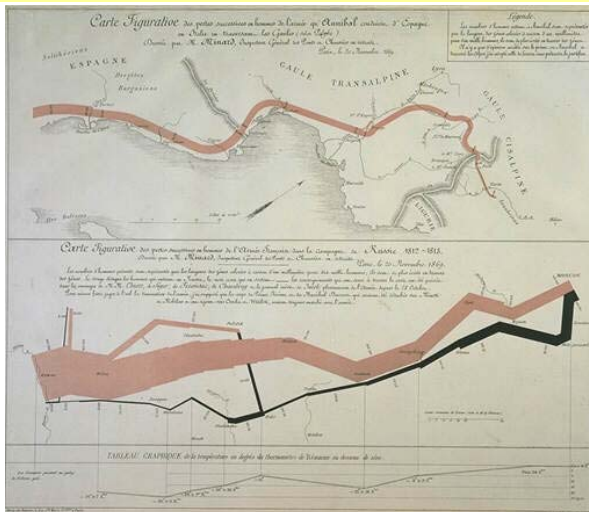


30

The March Re-Visited (1869)

Hannibal's retreat

Napoleon's 1812 campaign



31

Galton's discovery of weather patterns- Perhaps the most notable *purely graphic* discovery ever!

METEOROGRAPHICA,
 OR
METHODS OF MAPPING THE WEATHER;
 ILLUSTRATED BY UPWARDS OF 600 PRINTED AND LITHOGRAPHED DIAGRAMS
 REFERRING TO
THE WEATHER OF A LARGE PART OF EUROPE,
 During the Month of December 1861.
 BY FRANCIS GALTON, F.R.S.

(Galton, 1863)

32

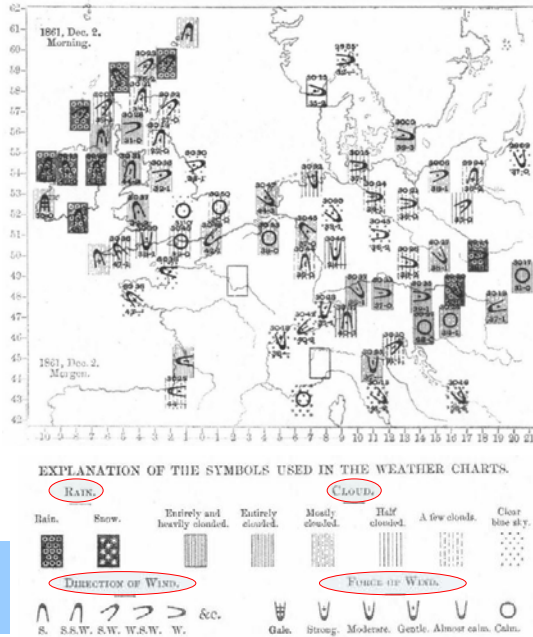
Method: All weather stations across Europe asked to record data 3x/day for all of Dec., 1861

Data: recordings of barometric pressure, wind dir/speed, rain, temp., cloud: 3x/day, 50 weather stations in Europe.

Graphic analysis: 3x31=93 maps, each with multivariate glyphs showing all variables

Visual ideas:

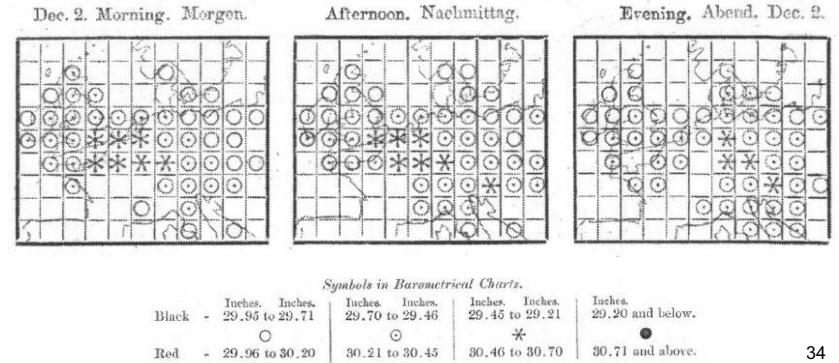
- Iconic symbols
- Multivariate glyphs (stamps!)



Visual abstraction → Patterns

How to see patterns of geographical variation over time?

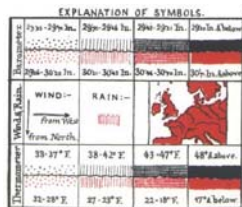
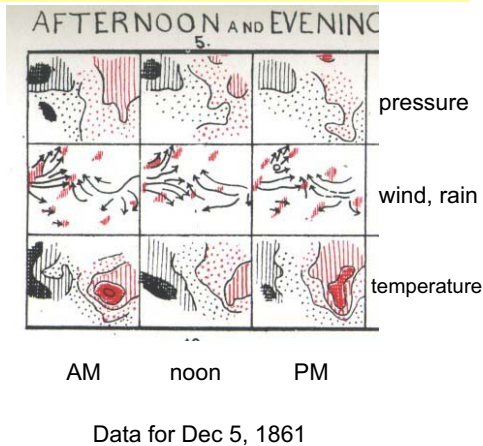
- Iconic symbols on a geographical grid
- “Small multiples:” separate graphs laid out for direct comparison



Visual abstraction → Patterns

What varies with what, over time and space?

- mini, abstract maps: vars x TOD
- iso-contours, shading to show equivalence
- arrows to show wind direction

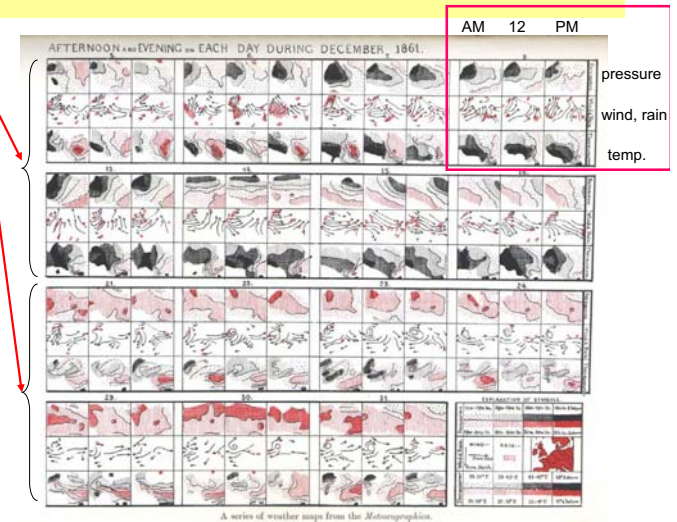


The large picture → Insight

Pattern:
 Low pressure (black) in early Dec. → CCW wind
 High pressure (red) in late Dec. → CW wind

Graphic: 3x3x31 grid, mapping {pressure, wind/rain, temperature} x {AM, 12, PM} x day {1:31}

(try this with your software!)



Visual insight → Theory

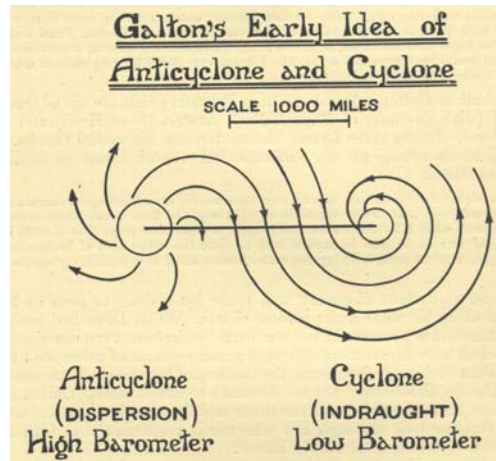
Visual insight from 93 (3x31)

high-D graphs:

- Changes in wind dir w/ pressure over time
- → Winds revolve inwardly (CCW) in low pressure areas—as in a cyclone;
- → revolve outwardly (CW) in high pressure areas—“anti-cyclone”

Theory:

- Explained by Dove's 'Law of Gyration'
- Prediction: reversed pattern (CW/CCW) in southern hemisphere – confirmed!

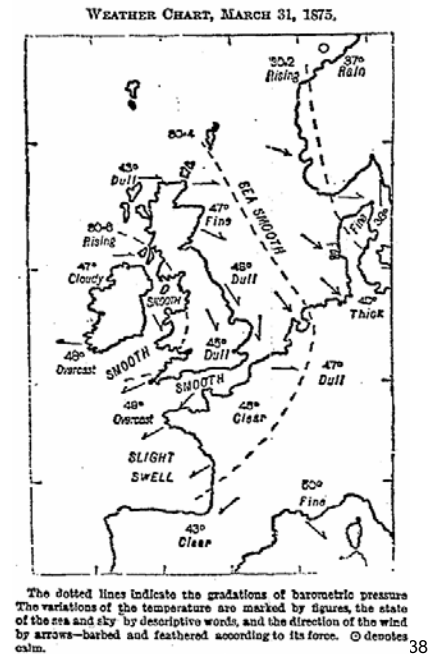


37

Theory → Practice

The first modern weather map,
London Times, Apr. 1, 1875

Galton did for weathermen what Kepler did for Tycho Brahe. This is no small accomplishment. (Wainer 2005)



38

Statistical atlases: Data → practice, national identity & graphical excellence

- Collection of gov't statistics on pop., trade, moral & political issues widespread in Europe & US, starting ~ 1820
- Statistical albums ~ 1870—1910
 - France: *Album de Statistique Graphique*: 1879-1899
 - USA: Census atlases: 1870/80/90
 - Germany: local albums (Berlin, Frankfurt, etc.)
 - Switzerland: *Atlas graphique de la Suisse*: 1897, 1914
 - Others: Latvia, Romania, Bulgaria, etc.

39

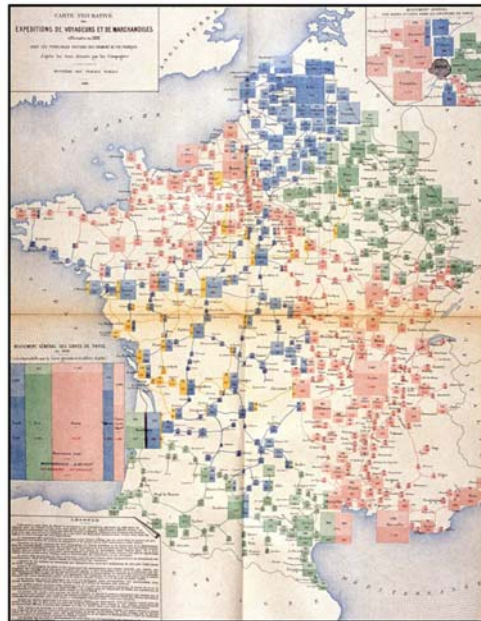
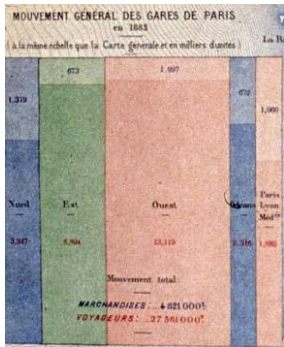
Album de statistique graphique

- Published by the Statistical Graphics Bureau, Ministry of Public Works, Émile Cheysson, director
- 18 volumes: 1879-1899, 12—34 plates each, ~ 11"x17" pages
- Graphic forms:
 - Flow maps (simple, double, multi)
 - Pie maps, star, radial, polar time-series, proportional circles
 - Mosaic maps, anamorphic maps, planetary diagrams
 - Choropleth, bi-polar scales
 - Charts: line, bar, time-series
- Formats: 1x1, 2x1, 2x2, 3x2, ...
- Themes:
 - Recurrent: railroads, navigation, transport (B&B)
 - Occasional: agriculture, Paris, expositions, ...
- Pinnacle of the Golden Age: exquisite sampler of all known graphic forms!

40

Recursive multi-mosaic map

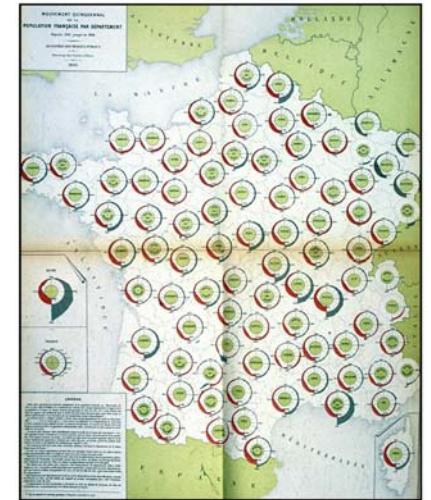
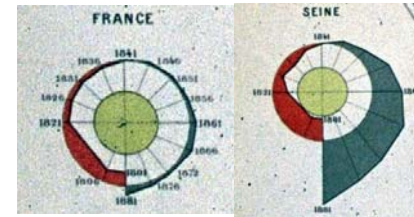
Distribution of passengers and goods from the Paris railways to the rest of France [Album, 1884, pl. 11]



Album de statistique graphique

Spiral time-series on a map

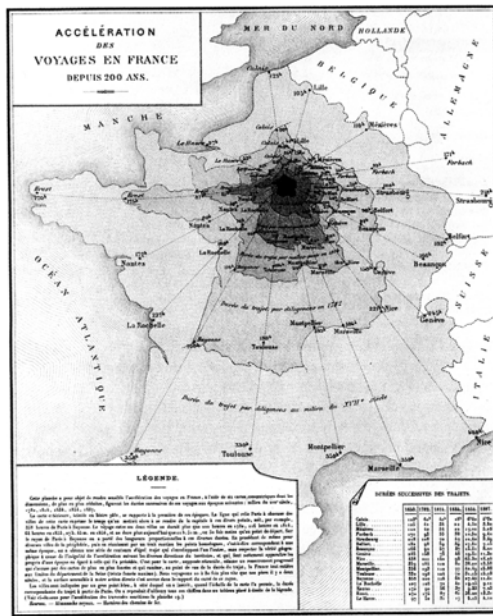
Changes in the population of France from 1801—1881, by department [Album, 1881, plate 25]



Anamorphic map

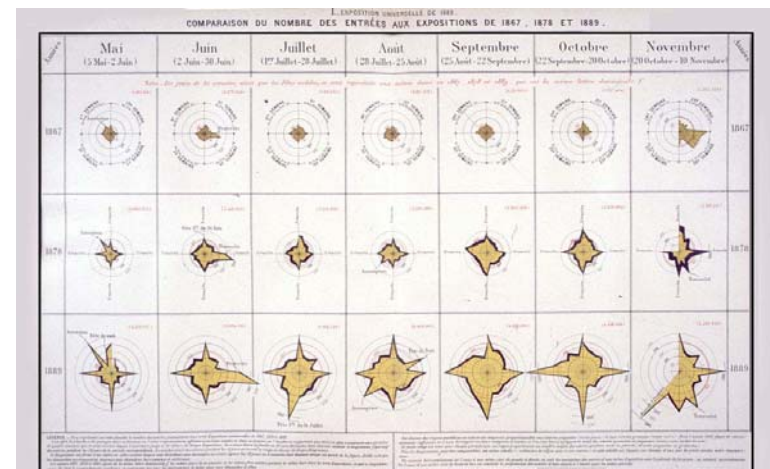
Shrinking France to show change in travel time over 200 years [Album, 1888, plate 8]

DURÉES SUCCESSIVES DES TRAJETS.						
	1650.	1789.	1814.	1834.	1854.	1887.
Caen	128 ^h	60 ^h	40 ^h	25 ^h	15 ^h	12 ^h
Lille	105	40	24	18	10	8
Münster	110	40	24	18	10	8
Ferbach	171	95	55	38	20	15
Strasbourg	118	70	47	30	16	12
Belfort	185	98	59	39	21	15
Bouayon	166	91	57	37	20	14
Genève	115	40	24	18	10	8
Nice	138	61	38	24	13	10
Marseille	155	78	48	30	16	12
Montpellier	135	68	41	26	14	10
Toulouse	130	65	40	25	13	10
Bayonne	158	80	48	30	16	12
La Rochelle	187	105	64	41	22	16
Nantes	179	90	56	37	20	14
Brest	170	85	51	32	18	13
Le Havre	97	50	31	17	9	7



Two-way table of star/radar diagrams

Attendance at the universal exhibitions in 1867, 1878, 1889 (rows), by month (cols) and days (rays). [Album, 1889, plate 21]

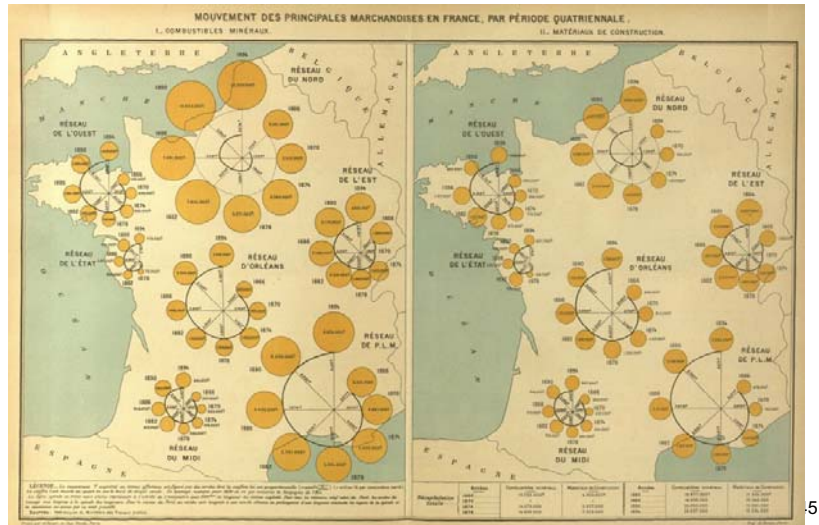


Planetary diagrams

Movement of principal merchandise by region. Spiral ~ distance; circles ~ tonnage
[Album, 1895, plate 9]

Combustible minerals

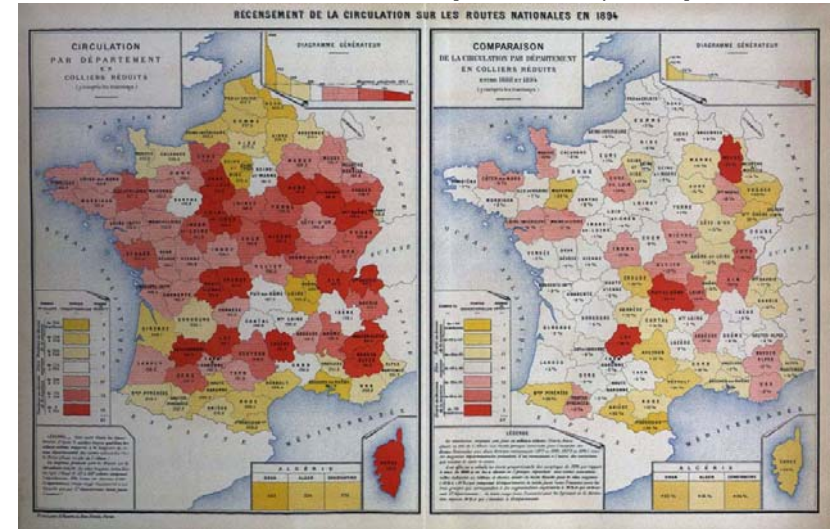
Construction materials



5

Classed choropleth maps, bipolar color scale

Circulation on the national roads in 'colliers réduits'
Left: 1894; Right: % change, 88-94
[Album, 1895, plate 21]



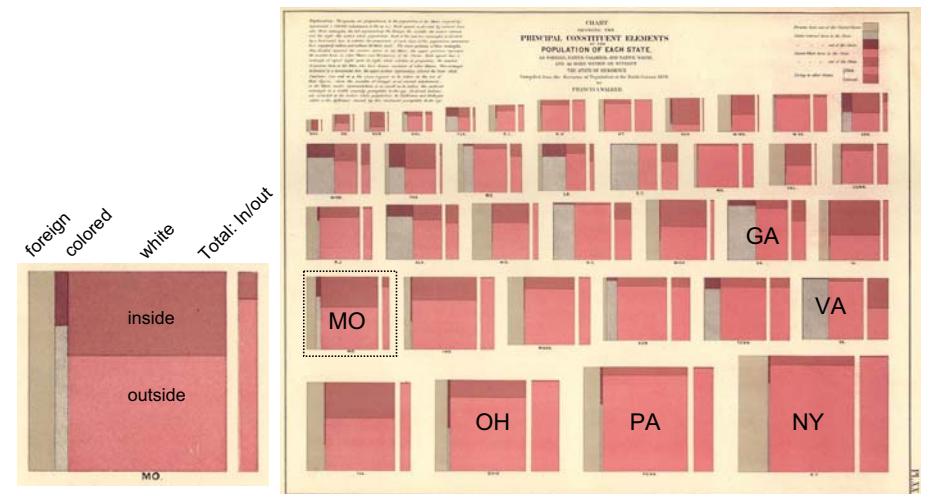
U.S. Census Atlases

- *Statistical Atlas of the Ninth Census (1872)* – Francis Walker
 - 60 plates: First graphic portrait of the nation
 - Topics: geology, minerals, weather, pop. by ethnicity, wealth, literacy, death rates by age, sex, cause, rates of blindness, insanity, etc.
- *Tenth Census (1880)* – Henry Gannett
 - 151 plates
- *Eleventh Census (1890)* – Henry Gannett
 - 126 plates

47

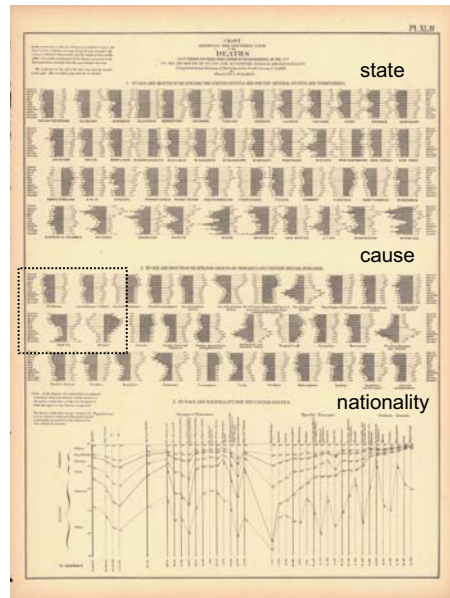
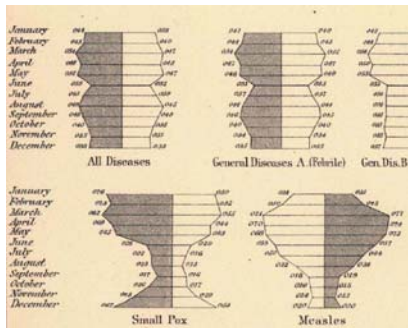
Mosaics/treemaps: Area ~ state population

State populations: Foreign born / Native colored / White + Born inside/outside
[Atlas, 1870, plate 20]



Bilateral histograms:
deaths (sex by month) ~
state, cause, nationality

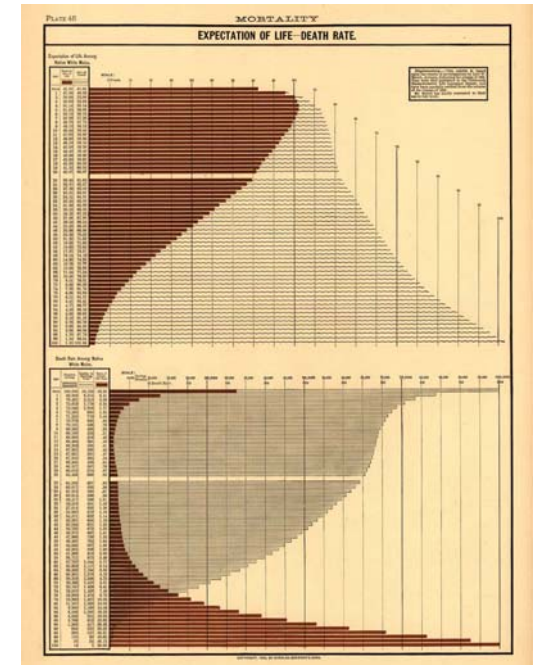
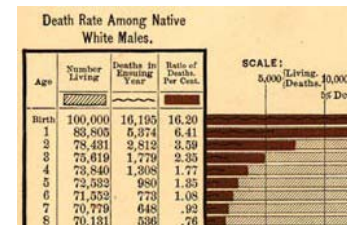
[Atlas, 1870, plate 44]



Multi-function bar & line graphs

Mortality: Life expectancy &
death rates by age, native
white males

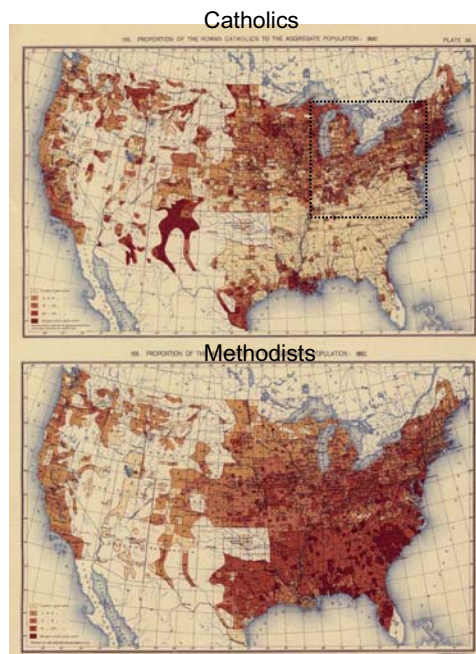
[Atlas, 1880, plate 40]



Comparative density maps

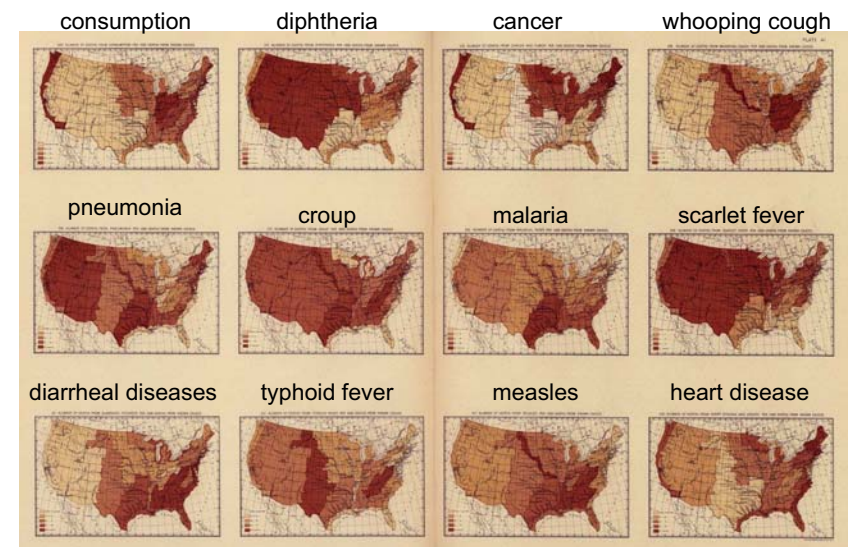
Proportions of Catholics and
Methodists in the total
population [Atlas, 1890, plate
36]

Detail (Catholics)



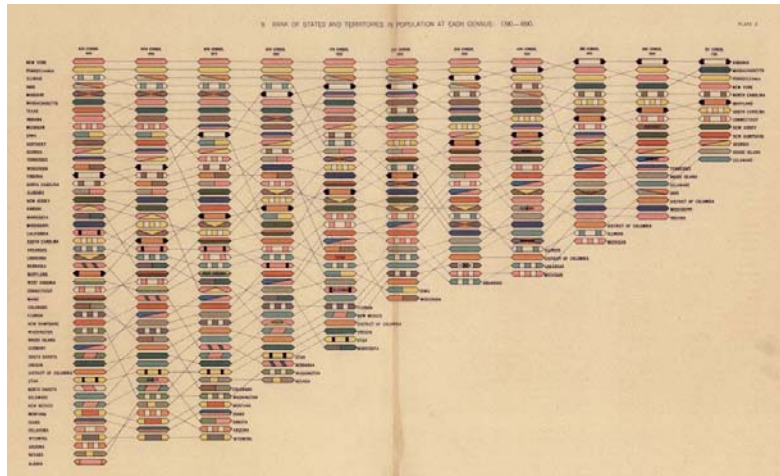
Comparative density maps

Deaths from diseases/1000
[Atlas, 1890, plate 41]



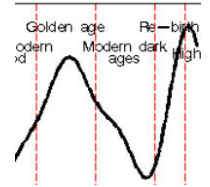
Linked parallel-coordinates time-series diagram

Rank of states & territories in each census, 1790—1890. [Atlas, 1898, plate 2]



Golden Age → Modern Dark Ages

- Statistics: enthusiasm for graphics replaced by rise of quantification
 - Statistical models (regression, correlation)
 - Estimates \pm standard errors: precise!
- Few innovations, but popularization
 - College courses, text books
- Some significant graphical discoveries
 - E.W. Maunder (1904): “butterfly diagram” of sunspots
 - Hertzsprung-Russell (1911) diagram: stellar physics
 - Henry Moseley (1913): atomic number



54

Conclusions

The only new thing... is the history you don't know – Harry Truman

- Modern data visualization has deep roots:
 - Cartography
 - Statistics
 - Data collection
 - Visual thinking
 - Technology
- The Golden Age
 - Qualitatively distinct, deserves recognition
 - Works of unparalleled beauty & scope
 - Thematic maps & diagrams often aided each other

55